

Useful Formulae:

Rayleigh-Jean's Law:	Intensity = $(8\pi\nu^2/c^3) kT$
Planck Radiation Law:	$8\pi h\nu^3/kT * (\exp(h\nu/kT)-1)^{-1}$
Wein's Law:	$\lambda_{\max} T = 2.897*10^{-3} \text{ mK}$
Stefan's Law:	$W = \sigma T^4$
Balmer Formula:	$\lambda = 364.6 n^2 / (n^2-4)$
Bohr Radii:	$r = n^2 a_0$
Hydrogen Energy:	$E = -13.6 / n^2$
Mode Spacing:	$\Delta\nu = c/2L$
Rate equations:	$r = dN/dt = W N$
Pumping probability:	$W = \sigma I/h\nu$
Level lifetime:	$\tau = 1/(\Sigma A)$

Minimum pump energy: $P_{\text{minimum}} = dN_{\text{ULL}}/dt V h\nu_{\text{mp}}$
Differential solution: $dN_{\text{ULL}}/dt = -1/\tau N_{\text{ULL}}$

Laser Rate Equations: $r_{\text{absorption}} = B_{12}N_1\rho$
 $r_{\text{stimulated}} = B_{21}N_2\rho$
 $r_{\text{spontaneous}} = A_{21}N_2$
 $A_{21} = 1/\tau_{21}$
 $r_{\text{stimulated}} / r_{\text{spontaneous}} = c^3\rho/8\pi h\nu^3s$
 $r_{\text{stimulated}} / r_{\text{absorption}} = N_2 / N_1$

Grating Formula: $d\sin\theta = m\lambda$

Thermal Energy: kT

Gain coefficient: $g = \Delta N \sigma_0$

Power Gain: $P_{\text{OUT}} = P_{\text{IN}} e^{gX}$

Planck's Relationship: $E = h\nu = \frac{hc}{\lambda}$

Boltzmann's Law: $N = N_0 e^{\frac{-E}{kT}}$

Cavity Radiation: $\rho = \frac{8\pi h\nu^3}{c^3} \frac{1}{e^{\frac{E}{kT}} - 1}$

Saturation Intensity: $I_{\text{sat}} = \frac{h\nu}{\sigma_0\tau}$

Fresnel equation:
(at 90 degrees) $R = \left(\frac{n_1 - n_2}{n_1 + n_2}\right)^2$

Fresnel equation: $R_p = \left(\frac{n \cos\theta_i - \cos\theta_r}{n \cos\theta_i + \cos\theta_r}\right)^2$

Linewidth: $\Delta\nu = 2\nu_0 \sqrt{\frac{2kT \ln(2)}{Mc^2}}$

Snell's Law: $\frac{\sin\theta_i}{n_r} = \frac{\sin\theta_r}{n_i}$

Threshold Gain:
(simple configuration) $g_{\text{threshold}} = \gamma + \frac{1}{2x} \ln\left(\frac{1}{R_1 R_2}\right)$

Saturated Gain: $g_{\text{sat}} = \frac{g_0}{1 + \frac{\rho}{\rho_{\text{sat}}}}$

Threshold Temp: $I_{\text{TH}} = I_0 e^{\frac{-\Delta T}{T_0}}$

Junction Temp: $T_{\text{Junction}} = T_{\text{amb}} + R_\theta \times P$

Constants and Conversions:

1eV = 1.602E-19J

0 C = 273.15 K

k = Boltzmann's constant (1.38 * 10⁻²³ J/K)

h = Planck's constant (6.626 * 10⁻³⁴ Js)

σ = Stefan-Boltzmann constant (5.67*10⁻⁸ Wm⁻²K⁻⁴)

c = Speed of Light (3*10⁸ m/s)

a₀ = Bohr radius (5.29*10⁻¹¹ m)

1 mole (Avogadro's number) = 6.02*10²³ atoms/molecules

Indices of Refraction: Quartz = 1.46, Glass = 1.51

Atomic masses: Neon = 20 amu, Argon = 38 amu, Helium = 4 amu, Cadmium=112 amu, CO₂ = 44 amu